THE UNIVERSITY



OF HONG KONG

Institute of Mathematical Research Department of Mathematics

Geometry and Physics of Duality

Workshop including the Hong Kong Geometry Colloquium (morning session)

Saturday, 29 November, 2014 Room 210, Run Run Shaw Building, HKU

10:00 – 11:00 **Peter Bouwknegt** (Australian National University, Canberra)

Spherical T-duality

Abstract: T-duality is an equivalence of String Theories on manifolds which are circle (or more generally, torus) bundles equipped with a background flux. Mathematically it provides an isomorphism for certain twisted cohomologies and K-theories for these manifolds. In this talk I will briefly review T-duality for circle bundles (U(1)-bundles), and then discuss a recent generalization to 3-sphere bundles (SU(2)-bundles), with applications to 7-twisted cohomologies and K-theories and the homotopy groups of 3-spheres. This talk is based on joint work with Jarah Evslin and Mathai Varghese [arXiv:1405.5844/1409.1296].

Coffee / Tea Break

11:30 – 12:30 Varghese Mathai (University of Adelaide, Adelaide)

Exotic twisted equivariant cohomology of loop spaces, twisted Bismut-Chern character and T-duality

Abstract: Fei Han and I define exotic twisted circle-equivariant cohomology for the loop space LZ of a smooth manifold Z via the invariant differential forms on LZ with coefficients in the (typically non-flat) holonomy line bundle of a gerbe, with differential an equivariantly flat superconnection. We introduce the twisted Bismut-Chern character form, a loop space refinement of the twisted Chern character form, which represent classes in the completed periodic exotic twisted circle-equivariant cohomology of LZ. We establish a localisation theorem for the completed periodic exotic twisted circle-equivariant cohomology for loop spaces and apply it to establish T-duality in a background flux in type II String Theory from a loop space perspective.

Lunch Break

14:30 – 15:30 Jae-Suk Park (Center for Geometry and Physics, POSTECH, Pohang)

When two quantum field theories are physically equivalent ?

Abstract: Quantum field theory often comes endowed with a physically natural duality, which leads to a duality or correspondence between different mathematical objects via some elaborate dictionary. Such correspondences are usually studied on a case-by-case basis, separately for each application. In this talk I will discuss an attempt to formulate quantum field theory based on certain algebraic homotopy category, such that the statement that two quantum field theories are physically equivalent has a mathematical definition.

Coffee / Tea Break

16:00 – 17:00 Kwok Wai Chan (The Chinese University of Hong Kong, Hong Kong)

SYZ mirror symmetry for toric Calabi-Yau varieties

Abstract: I will discuss mirror symmetry for toric Calabi-Yau manifolds/orbifolds from the viewpoint of the Strominger-Yau-Zaslow (SYZ) conjecture. As an application, we obtain a proof of a conjecture by Gross and Siebert which gives an enumerative meaning to (inverse) mirror maps in terms of virtual counting of holomorphic disks. This talk is based on a series of joint works with Cheol-Hyun Cho, Siu-Cheong Lau, Conan Leung and Hsian-Hua Tseng.